



SHEET 2

Problem 1

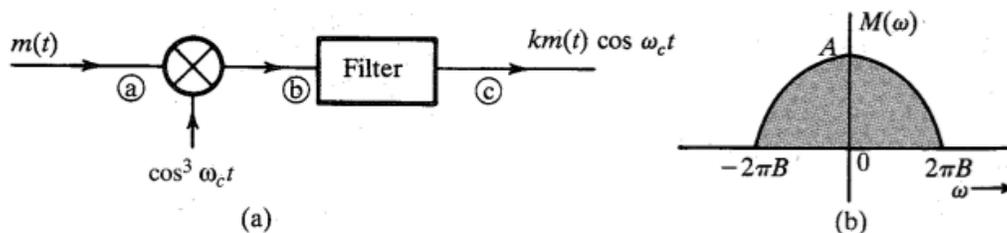
For each of the following baseband signals: (i) $m(t) = \cos 1000t$; (ii) $m(t) = 2 \cos 1000t + \cos 2000t$; (iii) $m(t) = \cos 1000t \cos 3000t$:

- (a) Sketch the spectrum of $m(t)$.
- (b) Sketch the spectrum of the DSB-SC signal $m(t) \cos 10,000t$.
- (c) Identify the upper sideband (USB) and the lower sideband (LSB) spectra.
- (d) Identify the frequencies in the baseband, and the corresponding frequencies in the DSB-SC, USB, and LSB spectra. Explain the nature of frequency shifting in each case.

Problem 2

You are asked to design a DSB-SC modulator to generate a modulated signal $km(t) \cos \omega_c t$, where $m(t)$ is a signal band-limited to B Hz. Figure P4.2-4 shows a DSB-SC modulator available in the stock room. The carrier generator available generates not $\cos \omega_c t$, but $\cos^3 \omega_c t$. Explain whether you would be able to generate the desired signal using only this equipment. You may use any kind of filter you like.

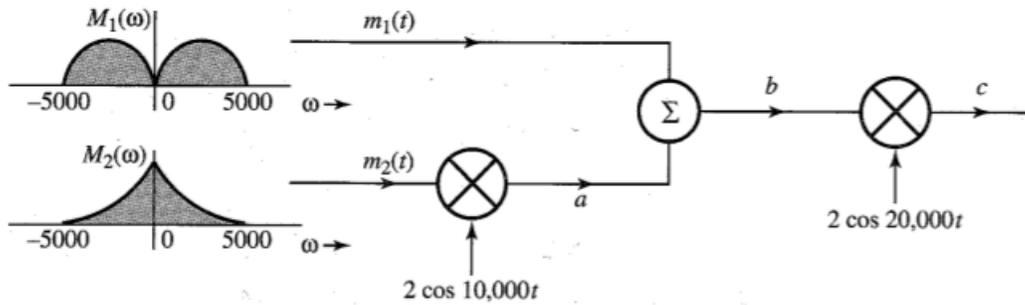
- (a) What kind of filter is required in Fig. P4.2-4?
- (b) Determine the signal spectra at points b and c , and indicate the frequency bands occupied by these spectra.
- (c) What is the minimum usable value of ω_c ?
- (d) Would this scheme work if the carrier generator output were $\cos^2 \omega_c t$? Explain.
- (e) Would this scheme work if the carrier generator output were $\cos^n \omega_c t$ for any integer $n \geq 2$?



Problem 3

Two signals $m_1(t)$ and $m_2(t)$, both band-limited to 5000 rad/s, are to be transmitted simultaneously over a channel by the multiplexing scheme shown in Fig. P4.2-8. The signal at point b is the multiplexed signal, which now modulates a carrier of frequency 20,000 rad/s. The modulated signal at point c is transmitted over a channel.

- (a) Sketch signal spectra at points a , b , and c .
- (b) What must be the bandwidth of the channel?
- (c) Design a receiver to recover signals $m_1(t)$ and $m_2(t)$ from the modulated signal at point c .

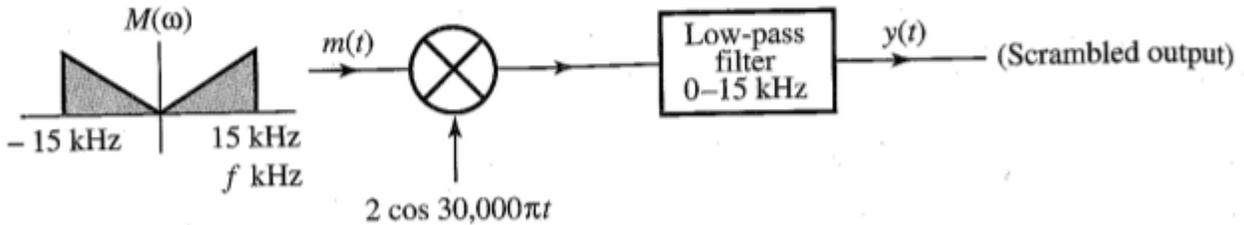


Problem 4

System shown in Fig. P4.2-9 is used for scrambling audio signals. The output $y(t)$ is the scrambled version of the input $m(t)$.

- (a) Find the spectrum of the scrambled signal $y(t)$.
- (b) Suggest a method of descrambling $y(t)$ to obtain $m(t)$.

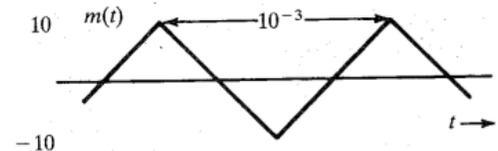
A slightly modified version of this scrambler was first used commercially on the 25-mile radio-telephone circuit connecting Los Angeles and Santa Catalina island.



Problem 5

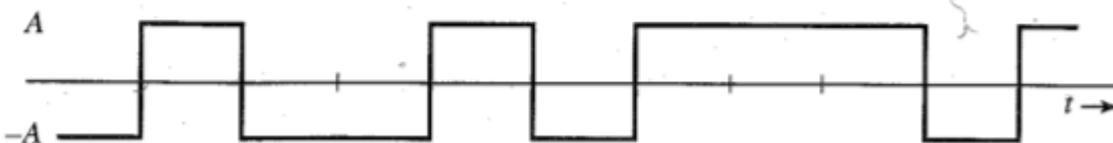
For the AM signal in Prob. 4.3-2 with $\mu = 0.8$:

- (a) Find the amplitude and power of the carrier.
- (b) Find the sideband power and the power efficiency η .



Problem 6

In the text, the power efficiency of AM for a sinusoidal $m(t)$ was found. Carry out a similar analysis when $m(t)$ is a random binary signal as shown in Fig. P4.3-7 and $\mu = 1$. Sketch the AM signal with $\mu = 1$. Find the sideband's power and the total power (power of the AM signal) as well as their ratio (the power efficiency η).



Problem 7

In the early days of radio, AM signals were demodulated by a crystal detector followed by a low-pass filter and a dc blocker, as shown in Fig. P4,3-8. Assume a crystal detector to be basically a squaring device. Determine the signals at points a , b , c , and d . Point out the distortion term in the output $y(t)$. Show that if $A \gg |m(t)|$, the distortion is small.

